

# FAIROD: Fairness-aware Outlier Detection

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<https://tinyurl.com/fairOD>

Longer version:  
<https://arxiv.org/pdf/2012.03063.pdf>

Fourth AAAI /ACM Conference on  
**Artificial Intelligence,  
Ethics, and Society**



Carnegie Mellon University  
**HeinzCollege**

**Snap Inc.**

# What is an outlier?

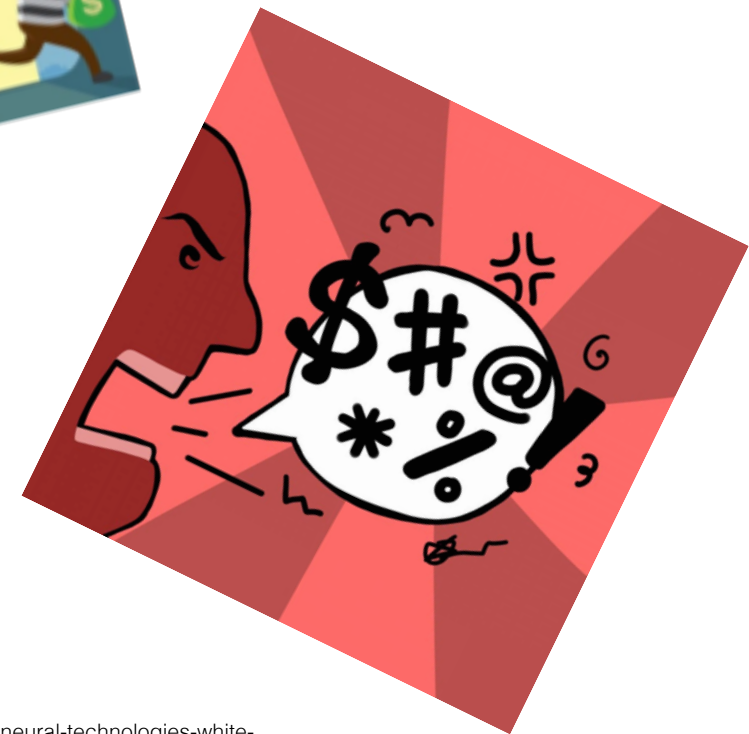
Observations that...

- “...are **inconsistent** with the remainder...”  
[Barnett&Lewis'94]
- “... deviate so much ... as to arouse suspicions ... they were generated by a **different mechanism**”  
[Hawkins '80]
- “... **deviate markedly** from other members of sample in which it occurs”  
[Grubbs '69]



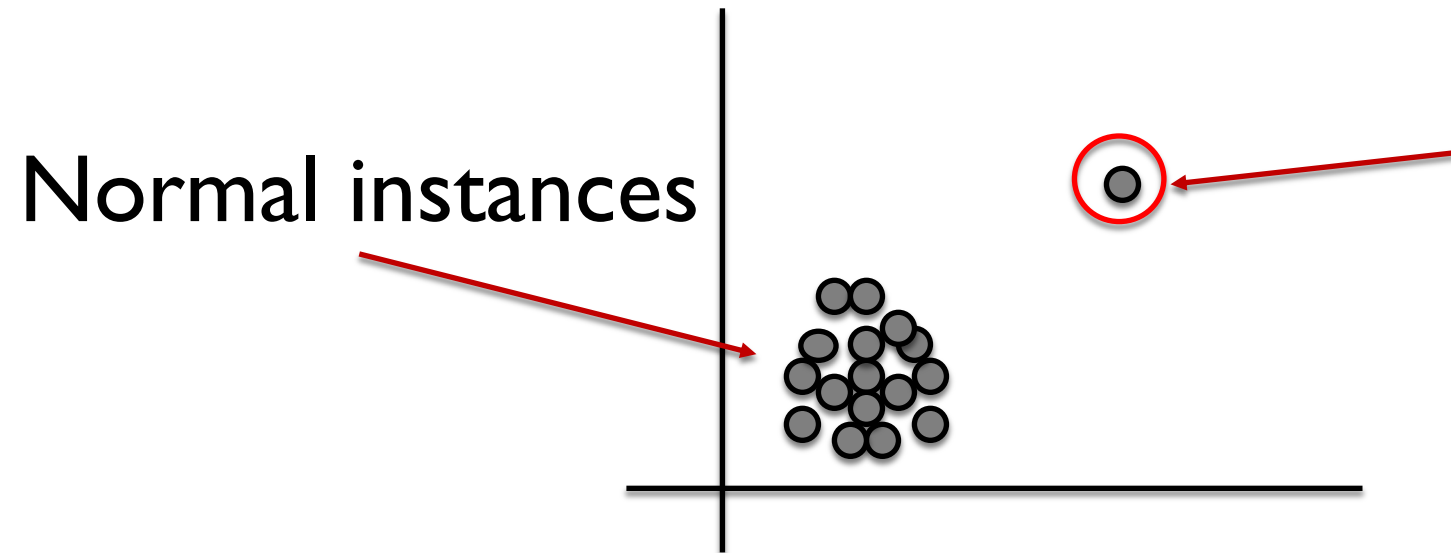


# Outlier Detection: Use-cases



Sources: <https://towardsdatascience.com/detecting-hate-tweets-twitter-sentiment-analysis-780d8a82d4f6>, <https://www.google.com/url?q=https://www.the-digital-insurer.com/insurance-fraud-digital-age-neural-technologies-white-paper/&sa=D&source=hangouts&ust=1620381203046000&usg=AFQjCNGpeSoWM0xriR0YhGq3vXzrhdisLg>, [https://www.google.com/url?q=https://www.internetmatters.org/hub/news-blogs/stopping-the-spread-of-fake-news-on-popular-online-platforms/&sa=D&source=hangouts&ust=1620381203046000&usg=AFQjCNHTmHYACxrcOX0A-vTMcTpM3\\_Fxw](https://www.google.com/url?q=https://www.internetmatters.org/hub/news-blogs/stopping-the-spread-of-fake-news-on-popular-online-platforms/&sa=D&source=hangouts&ust=1620381203046000&usg=AFQjCNHTmHYACxrcOX0A-vTMcTpM3_Fxw), <https://www.investopedia.com>, <https://traderdefenseadvisory.com/>, <https://www.google.com/url?q=https://blog.volkovlaw.com/2015/01/healthcare-fraud-aggressive-enforcement-strategies/&sa=D&source=hangouts&ust=1620386116751000&usg=AFQjCNGw2wgs6uMWfIB8D2L6qXeJWPnibg>

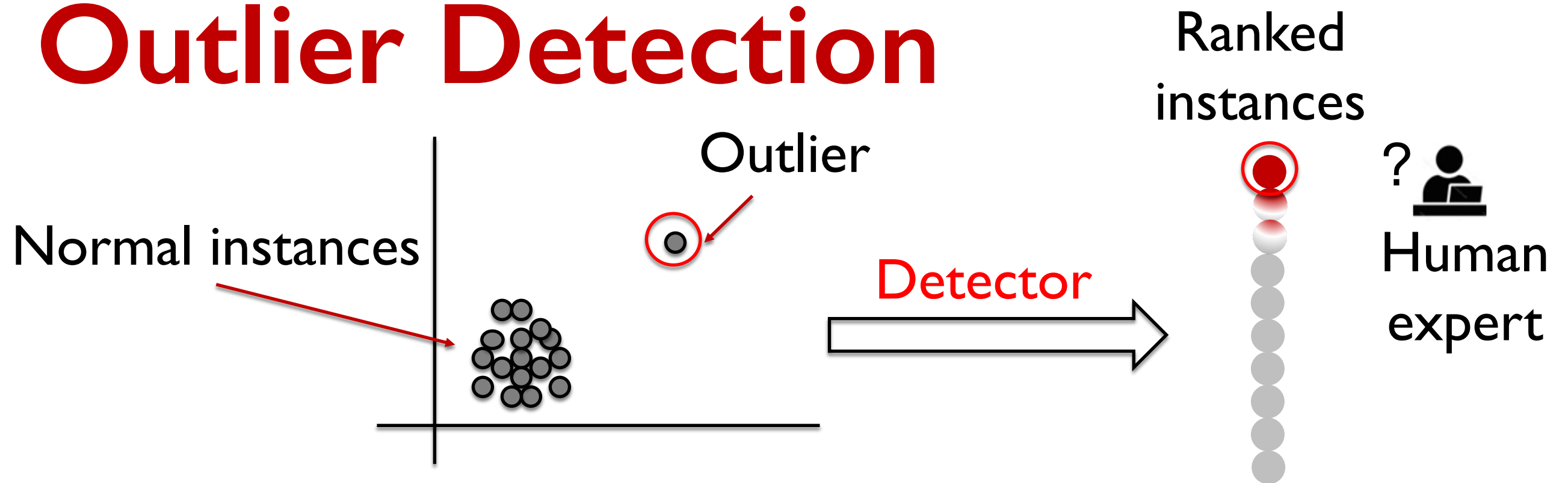
# Outlier Detection



Inconsistent with normal observations

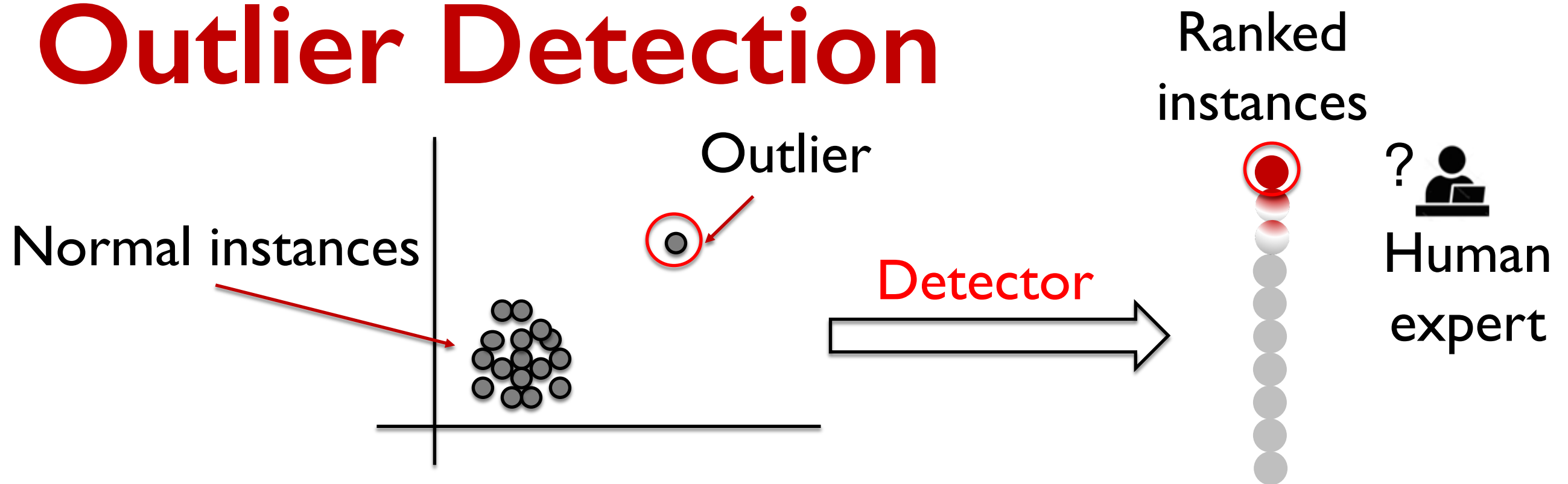


# Outlier Detection



- designed to spot/flag rare, minority samples
  - e.g. suspicious activity, abnormal heart rate, etc.

# Outlier Detection



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  - e.g. suspicious activity, abnormal heart rate, etc.
- facilitates auditing (“*policing*”) by human experts
  - e.g. Stop-and-frisk in automated surveillance flagged instances
  - Human-labeled data for downstream learning tasks



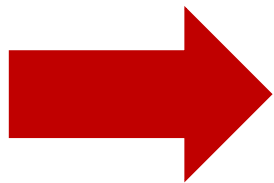
# Outlier Detection



- designed to spot/flag rare, minority samples
  - e.g. suspicious activity, abnormal heart rate etc.
- facilitates auditing (“*policing*”) by human experts
  - e.g. stop-and-frisk in automated surveillance flagged instances
  - human labeled data for downstream learning tasks

# Roadmap

- Introduction

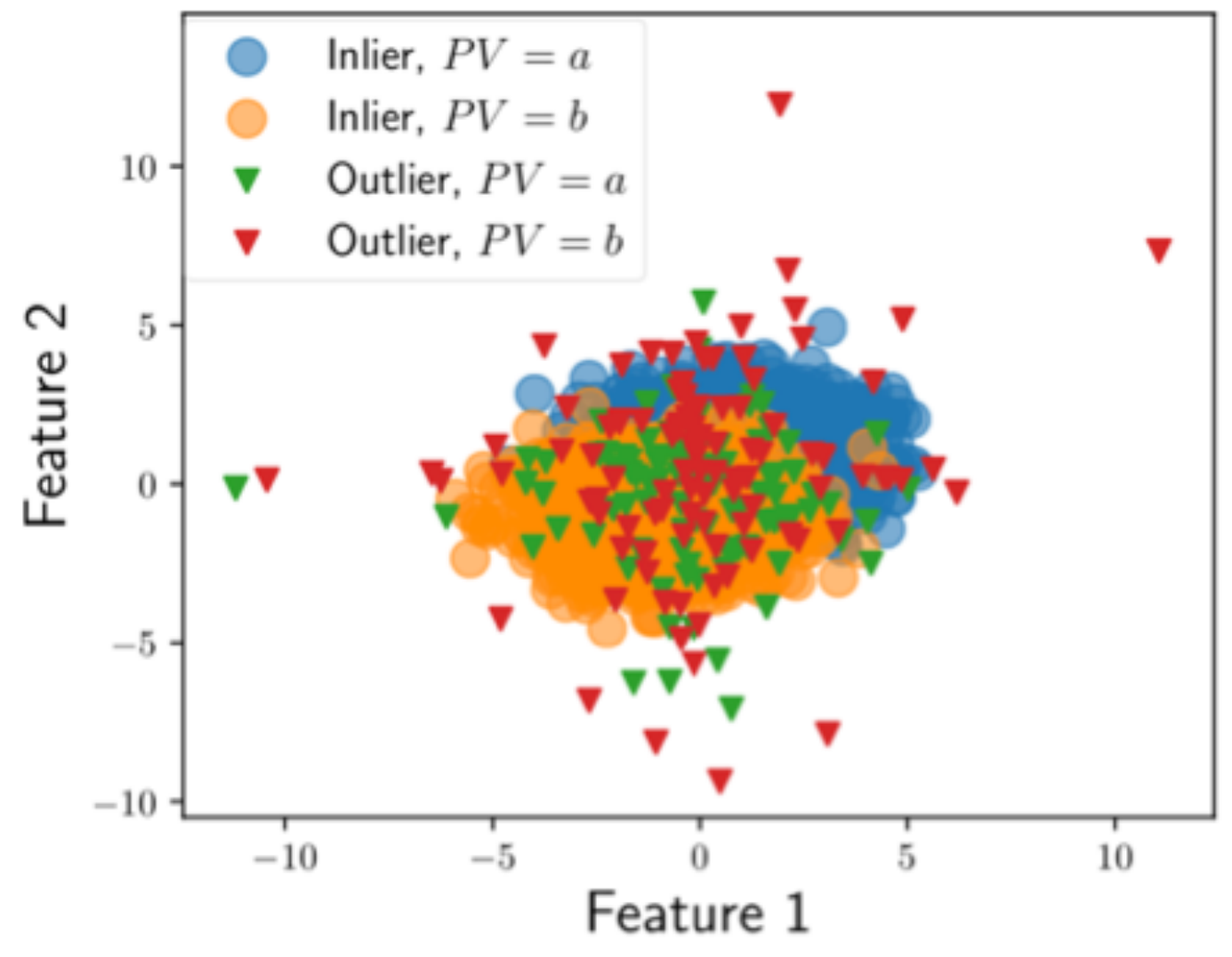


- Problem: Fairness in OD
- Desiderata
- Fairness-aware OD
- Evaluation



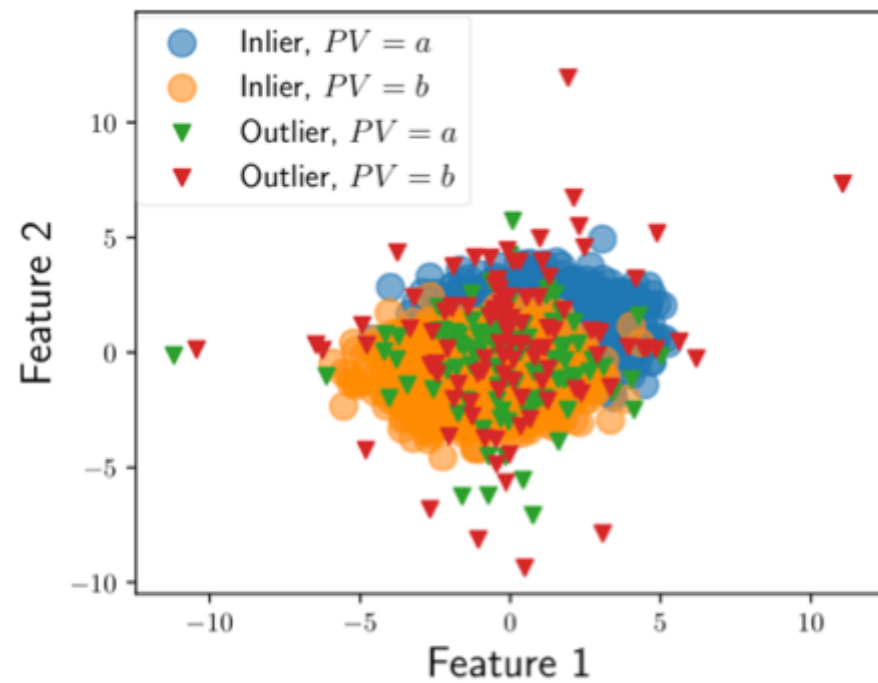


# Bias in Outlier Detection

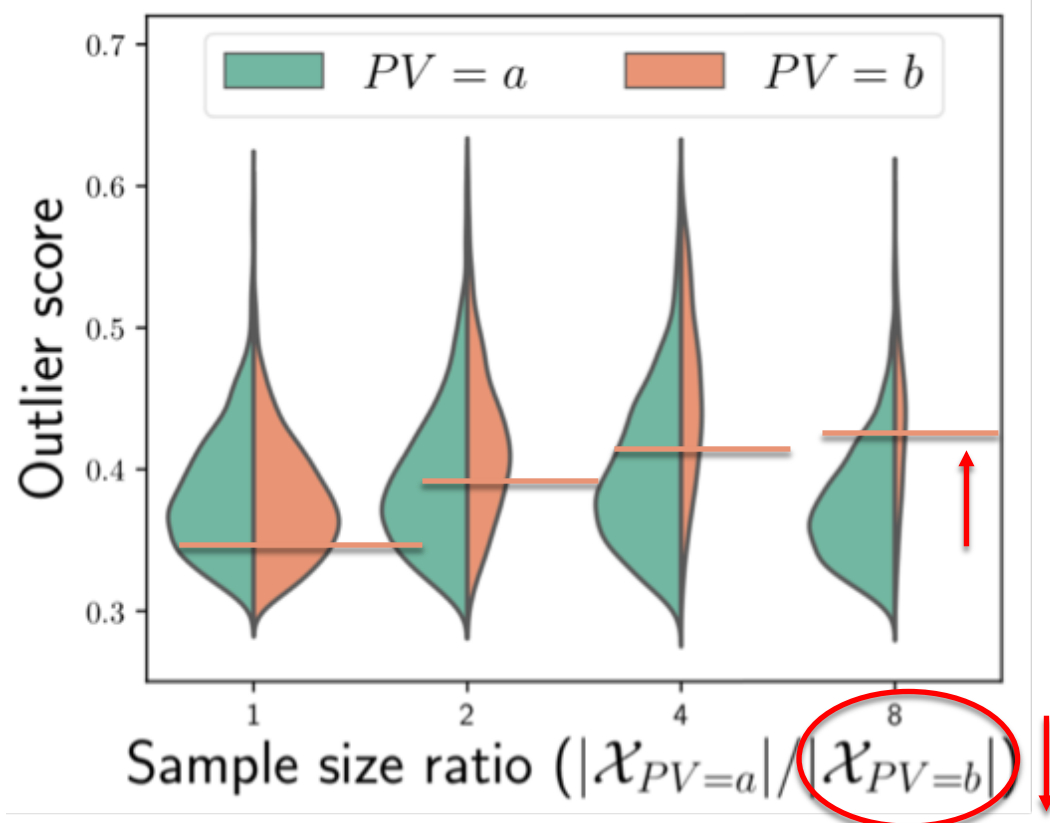


- Simulated dataset
  - equal sized groups
  - groups induced by  $PV = a$  and  $PV = b$

# Bias in Outlier Detection



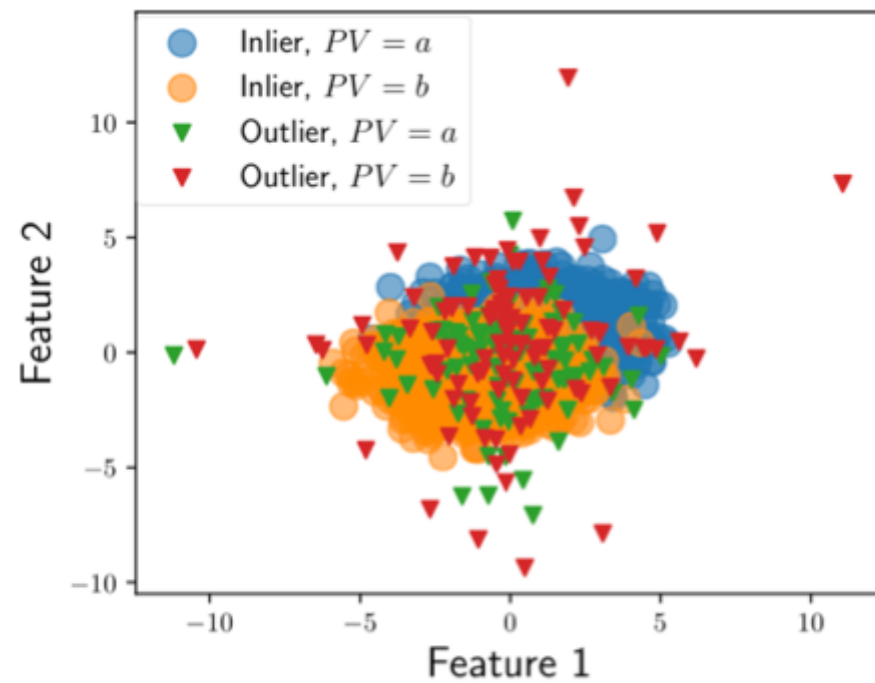
- Simulated dataset
  - equal sized groups
  - groups induced by  $PV = a$  and  $PV = b$



Higher outlier scores as sample size of  $PV = b$  is decreased

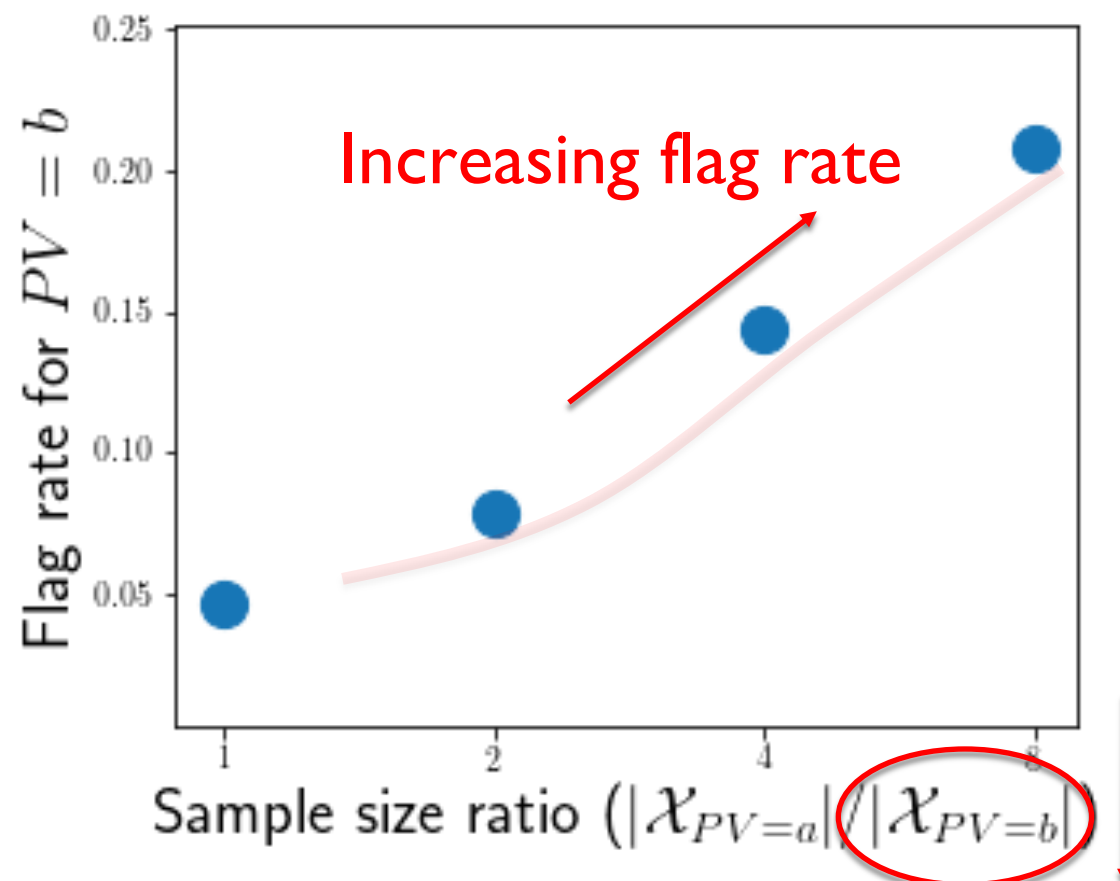


# Bias in Outlier Detection



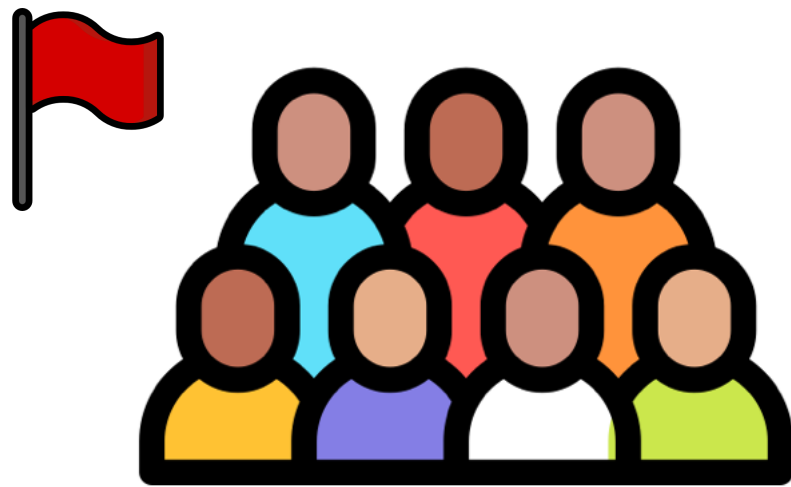
- Simulated dataset
  - equal sized groups
  - groups induced by  $PV = a$  and  $PV = b$

Corresponding flag rate for  $PV = b$  increases



# Bias in Outlier Detection

- Societal minorities may be statistical minorities
  - defined by protected variable (PV) :  
race/ ethnicity/gender/age etc.



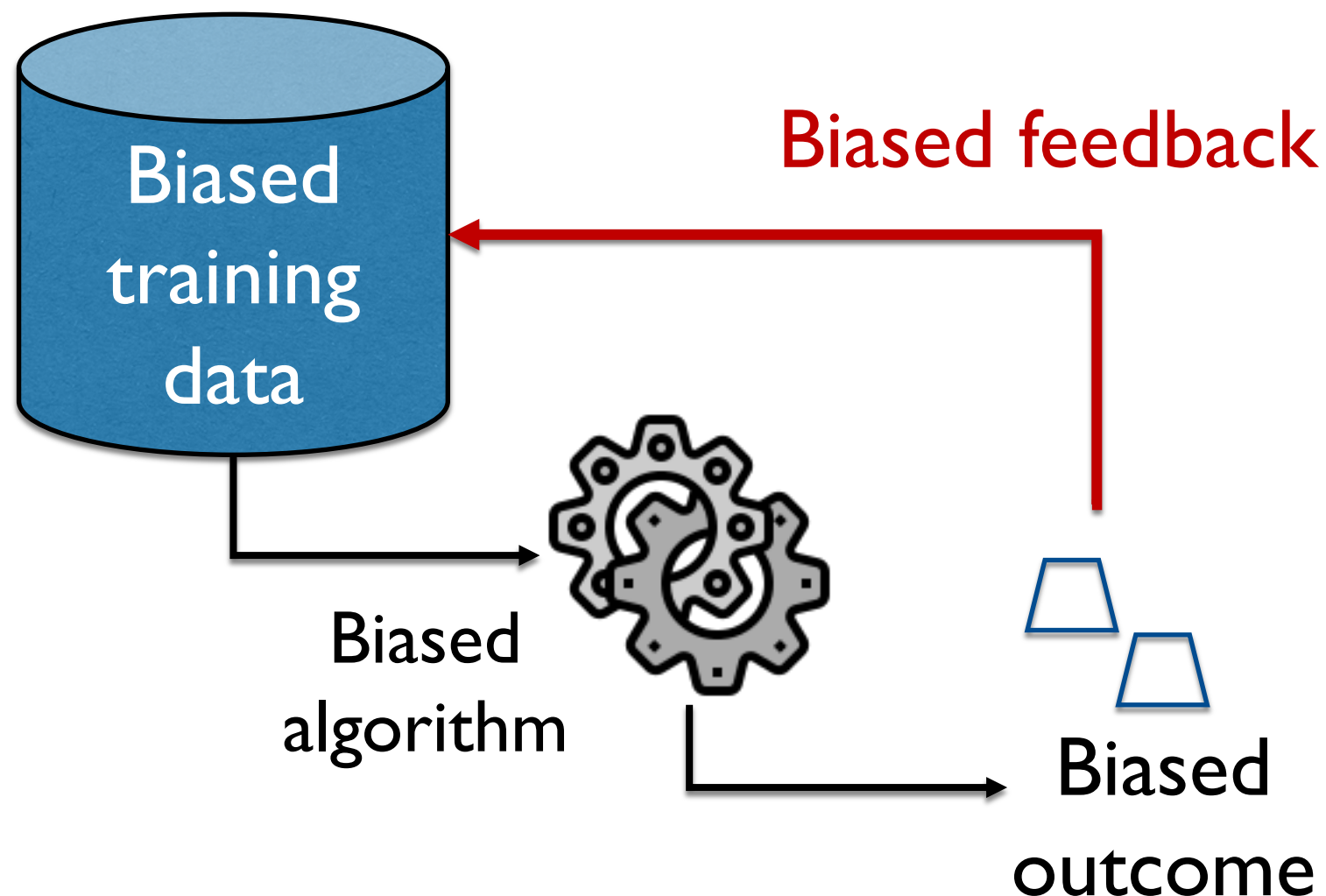
≠ riskiness



# Bias in Outlier Detection

- **Disparate Impact**

- Unjust flagging leads to “over-policing”
- Feedback loop results in further skewness



# Fair Outlier Detection

- Given:
  - Observations  $\mathcal{X} = \{X_i\}_{i=1}^N \subseteq \mathbb{R}^d$
  - $\mathcal{PV} = \{PV_i\}_{i=1}^N$ ,  $PV_i \in \{a, b\}$ 
    - $PV_i = a$  identifies majority group
- Build a **detector** that estimates outlier scores  $\mathcal{S}$  and assigns outlier labels  $\mathcal{O}$  s.t.
  - i. assigned labels and scores are **“fair”** w.r.t. the  $PV$
  - ii. **higher scores** correspond to **higher riskiness** encoded by the underlying (unobserved) true labels  $\mathcal{Y}$



# Fair Outlier Detection

- Given:

➤ Observations  $\mathcal{X} = \{X_i\}_{i=1}^N \subseteq \mathbb{R}^d$

***What constitutes a “fair” outcome in OD?***

➤  $PV_i = a$  identifies majority group

- Build a **detector** that estimates outlier scores  $\mathcal{S}$  and assigns outlier labels  $\mathcal{O}$  s.t.

i. assigned labels and scores are “**fair**” w.r.t. the  $PV$

ii. higher scores correspond to higher riskiness encoded by the underlying (unobserved) true labels  $\mathcal{Y}$



# Literature on Fairness in OD

- Algorithmic fairness – mostly for supervised ML
  - **Unsupervised** OD adds challenge
  - Numerous notions of fairness and associated incompatibility results
- Possible approach: **pre-processing**
  - **re-purpose (unsupervised) fair representation learning**
    1. PV-obfuscated/masked new embeddings
    2. Re-weighted/adjusted data distributions
  - **Issue:** an isolated/detached step to OD task at hand



# Literature on Fairness in OD

- Algorithmic fairness – mostly for supervised ML
  - Unsupervised OD adds challenge
  - Numerous notions of fairness and associated incompatibility results
- Countably-few work on fairness for OD
  1. [A Framework for Determining the Fairness of Outlier Detection.](#) [Ravi & Davidson, ECAI 2020]
    - ❖ Quantify/measure (detect) the (un)fairness of OD model outcomes **post hoc** (i.e. proceeding detection)
  2. [Fair Outlier Detection.](#) [P & Abraham, WISE 2020]
  3. [Towards Fair Deep Anomaly Detection.](#) [Zhang & Davidson, FAccT 2021]
  4. [Deep Clustering based Fair Outlier Detection.](#) [Song+, KDD 2021]
  5. [Fairness-aware Outlier Ensemble.](#) [Liu+, 2021 - unpublished]

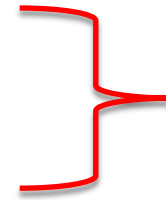
# Roadmap

- Introduction
- Problem: Fairness in OD
- ➔ • Desiderata
- Fairness-aware OD
- Evaluation



# Proposed Desiderata

D1. Detection effectiveness

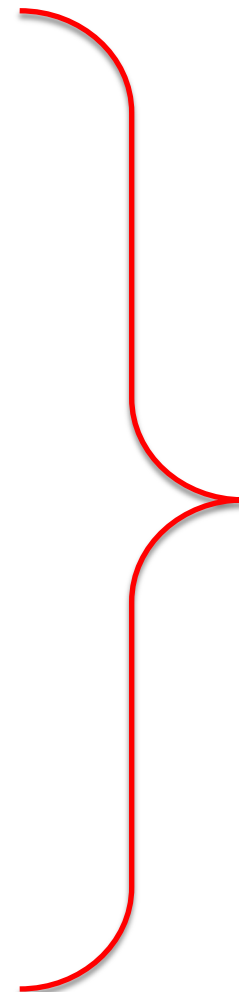


detection  
performance



D2. Treatment parity

D3. Statistical parity (SP)



fairness  
related



D4. Group fidelity

D5. Base rate preservation

# Proposed Desiderata



## **DI. Detection effectiveness** - accurate at detection

$$P(Y = 1 \mid O = 1) > P(Y = 1)$$

- related to detection performance



# Proposed Desiderata



D1. Detection effectiveness

**D2. Treatment parity** – decision avoids use of PV

$$P(O=1|X) = P(O=1|X, PV=v), \quad \forall v$$

- ensures OD-decisions are “blindfolded” to PV

# Proposed Desiderata



D1. Detection effectiveness

## **D2. Treatment parity** – decision avoids use of PV

$$P(O=1|X) = P(O=1|X, PV=v), \quad \forall v$$

- ensures OD-decisions are “blindfolded” to PV
- (!) may allow **discriminatory OD results** for **minority**:
  - due to several other features that **(partially-)redundantly encode** the PV (e.g. zipcode & race).
  - OD will use the PV indirectly, through **proxy** features.

# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

**D3. Statistical parity (SP)** – decision independent of PV

$$P(O=1 | PV=a) = P(O=1 | PV=b)$$

➤ a.k.a. demographic parity, or group fairness

# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

**D3. Statistical parity (SP)** – decision independent of PV

$$P(O=1|PV=a) = P(O=1|PV=b)$$

⇒ fraction of minority (majority) members in flagged set  
is the **same as**  
fraction of minority (majority) in overall population.

$$fr_a = fr_b \text{ (SP)} \iff P(PV = a|O = 1) = P(PV = a) \text{ and} \\ P(PV = b|O = 1) = P(PV = b) .$$

# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

**D3. Statistical parity (SP)** – decision independent of PV

$$P(O=1|PV=a) = P(O=1|PV=b)$$

$$\implies P(PV = a|O = 1) = P(PV = a) \text{ and}$$

$$P(PV = b|O = 1) = P(PV = b) .$$

- Derives from “**luck egalitarianism**” : [Carl Knight, 2009]  
counteract the distributive effects of “brute luck”  
– by redistributing equality to those who suffer through  
no fault of their own choosing of race, gender, etc.



# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

**D3. Statistical parity (SP)** – decision independent of PV

$$P(O=1 | PV=a) = P(O=1 | PV=b)$$

- permits “*laziness*”; may disadvantage some groups despite SP [Barocas et al.'2017]



PV ∈ {●, ●}



# Proposed Desiderata



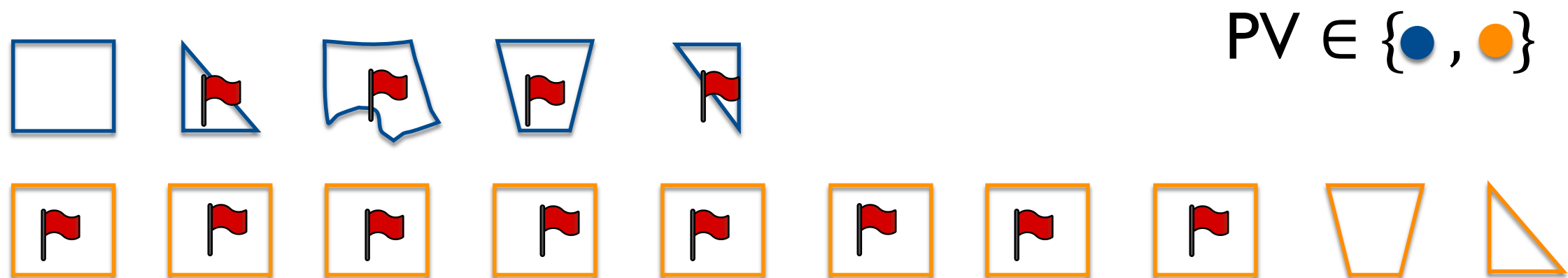
D1. Detection effectiveness

D2. Treatment parity

**D3. Statistical parity (SP)** – decision independent of PV

$$P(O=1 | PV=a) = P(O=1 | PV=b)$$

➤ permits “*laziness*” [Barocas et al.’2017]



# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

D3. Statistical parity (SP)

**D4. Group fidelity** – decision faithful to ground-truth

$$P(O=1|Y=1, PV=a) = P(O=1|Y=1, PV=b)$$

- penalizes “*laziness*”
- equivalent to the so-called Equality of Opportunity\*
- same true positive rate (TPR) for all groups

# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

D3. Statistical parity (SP)

**D4. Group fidelity** – decision faithful to ground-truth

$$P(O=1|Y=1, PV=a) = P(O=1|Y=1, PV=b)$$

- requires access to the ground-truth
  - unavailable for unsupervised OD task
- D3 (SP) and D4 are incompatible [Barocas et al.'2017]

# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

D3. Statistical parity (SP)

**D4. Group fidelity** – decision faithful to ground-truth

$$P(O=1|Y=1, PV=a) = P(O=1|Y=1, PV=b)$$

- **approx.:** enforce group-level rank preservation
- fidelity to **within-group ranking** from the *BASE* model
  - $\pi_{PV=v}^{BASE} = \pi_{PV=v}; \quad \forall v \in \{a, b\}$
  - $\pi$  denotes ranking



# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

D3. Statistical parity (SP)

D4. Group fidelity

**D5. Base rate preservation** – equal base rate  
in **flagged** instances and the **population**

$$P(Y = 1 | O = 1, PV = v) = \underbrace{P(Y = 1 | PV = v)}_{\text{Base rate/Prevalence for } PV = v}, \forall v \in \{a, b\}$$

**Base rate/Prevalence**  
for  $PV = v$

# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

D3. Statistical parity (SP)

D4. Group fidelity

**D5. Base rate preservation** – equal base rate  
in flagged instances and the population

$$P(Y = 1 | O = 1, PV = v) = P(Y = 1 | PV = v), \forall v \in \{a, b\}$$

➤ Incompatibility: given OD satisfies D1 and D3,  
it cannot also satisfy D5

*(See Claim 1 in the paper)*

# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

D3. Statistical parity (SP)

D4. Group fidelity

**D5. Base rate preservation** – equal base rate  
in flagged instances and the population

$$P(Y = 1 | O = 1, PV = v) = P(Y = 1 | PV = v), \forall v \in \{a, b\}$$

- relaxation: preservation of the ratio of base rates
  - Leads to overestimation of true group-level base rates (*Claim 2*)
- still, D5 cannot be enforced: relies on ground-truth

# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

D3. Statistical parity (SP)

D4. Group fidelity

D5. Base rate preservation

✓ Enforceable

✓ Enforceable via  
proposed proxy

✗ Can't be  
enforced



# Proposed Desiderata



D1. Detection effectiveness

D2. Treatment parity

✓ Enforceable

*Fair OD model follows the proposed desiderata  
D1 - D4.*

D4. Group fidelity

✓ Enforceable via  
proposed proxy

D5. Base rate preservation

✗ Can't be  
enforced



# Literature on Fairness in OD

- Countably-few work on fair OD
  1. **Fair Outlier Detection.** [P and Abraham, WISE 2020]
    - Seminal paper
    - **disparate treatment** (i.e. uses PV) at decision time (may be unlawful for some settings!)
    - prioritizes statistical parity (**SP**); may permit “laziness”
    - not end-to-end but rather **heuristic**
  2. **Towards Fair Deep Anomaly Detection.** [Zhang & Davidson, FAccT 2021]
    - focus on **SP**
    - **one-class** objective & **adversarial** training for **PV** prediction

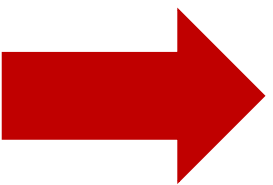


# Literature on Fairness in OD

- Countably-few work on fairness for OD
- 3. Deep Clustering based Fair Outlier Detection. [Song+, KDD 2021]
  - Again, sole focus on SP
- 4. Fairness-aware Outlier Ensemble. [Liu+, 2021; not publ.]
  - assumes the outlier scores “obtained from the **base** outlier ensemble method is an **optimal** result” (why do anything if this is true!)
  - notions of *group* fairness : focus on **SP** only & *individual* fairness : **similarity** “based on **original feature** values **excluding sensitive features**” (proxy variables!)

# Roadmap

- Introduction
- Problem: Fairness in OD
- Desiderata
- **Fairness-aware OD**
- Evaluation

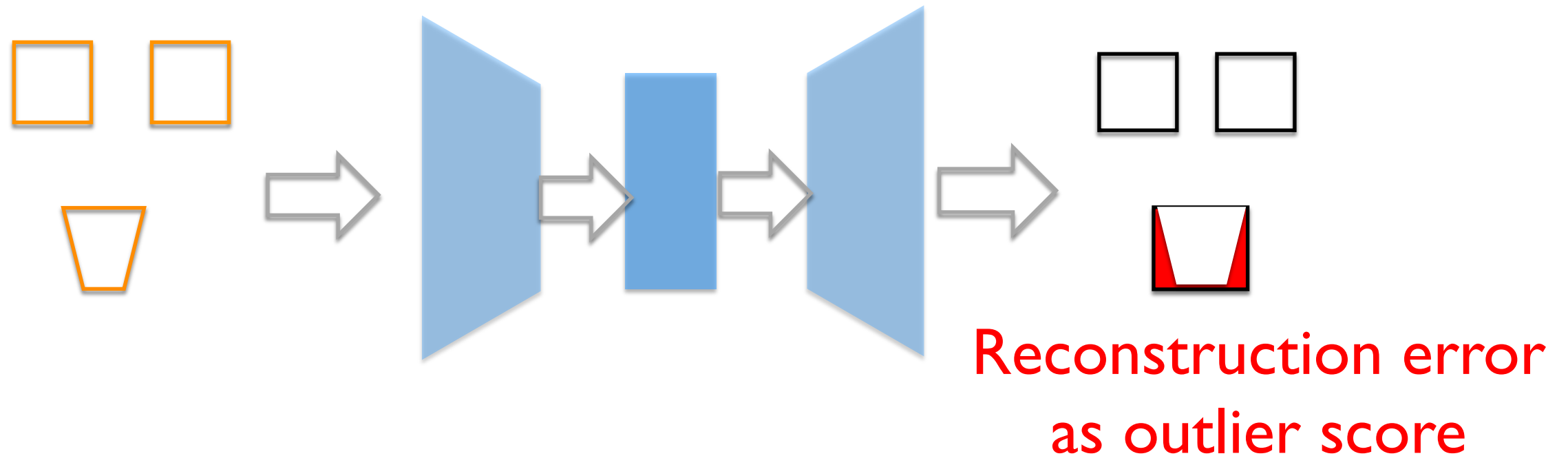


# Fairness-aware Outlier detection

- Given:
  - Observations  $\mathcal{X} = \{X_i\}_{i=1}^N \subseteq \mathbb{R}^d$
  - $\mathcal{PV} = \{PV_i\}_{i=1}^N$ ,  $PV_i \in \{a, b\}$ 
    - $PV_i = a$  identifies majority group
- Build a **detector** that estimates outlier scores  $\mathcal{S}$  and assigns outlier labels  $\mathcal{O}$  to achieve
  - i.  $P(Y = 1 \mid O = 1) > P(Y = 1)$  [D1]
  - ii.  $P(O=1 \mid X) = P(O=1 \mid X, PV=v), \forall v$  [D2]
  - iii.  $P(O=1 \mid PV=a) = P(O=1 \mid PV=b)$  [D3]
  - iv.  $\pi_{PV=v}^{\text{BASE}} = \pi_{PV=v}; \forall v$ , [D4]  
BASE is **fairness-agnostic** detector

# FAIROD

- Instantiates deep-autoencoder as BASE detector



- Minimizes the regularized loss:

$$\mathcal{L} = \alpha \underbrace{\mathcal{L}_{\text{BASE}}}_{\text{Reconstruction}} + (1 - \alpha) \underbrace{\mathcal{L}_{\text{SP}}}_{\text{Statistical Parity}} + \gamma \underbrace{\mathcal{L}_{\text{GF}}}_{\text{Group Fidelity}}$$

# FAIROD

$$\mathcal{L} = \alpha \underbrace{\mathcal{L}_{\text{BASE}}}_{\text{Reconstruction}} + (1 - \alpha) \underbrace{\mathcal{L}_{\text{SP}}}_{\text{Statistical Parity}} + \gamma \underbrace{\mathcal{L}_{\text{GF}}}_{\text{Group Fidelity}}$$

$$\mathcal{L}_{\text{BASE}} = \sum_{i=1}^N \|X_i - G(X_i)\|_2^2$$

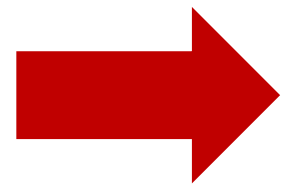
$$\mathcal{L}_{\text{SP}} = \left| \frac{\left( \sum_{i=1}^N s(X_i) - \mu_s \right) \left( \sum_{i=1}^N PV_i - \mu_{PV} \right)}{\sigma_s \sigma_{PV}} \right|$$

$$\mathcal{L}_{\text{GF}} = \sum_{v \in \{a, b\}} \left( 1 - \sum_{X_i \in \mathcal{X}_{PV=v}} \frac{2^{s^{\text{BASE}}(X_i)} - 1}{\log_2 \left( 1 + \sum_{X_k \in \mathcal{X}_{PV=v}} \text{sigm}(s(X_k) - s(X_i)) \right) \cdot IDC G_{PV=v}} \right)$$

See paper for details : <https://arxiv.org/pdf/2012.03063.pdf>

# Roadmap

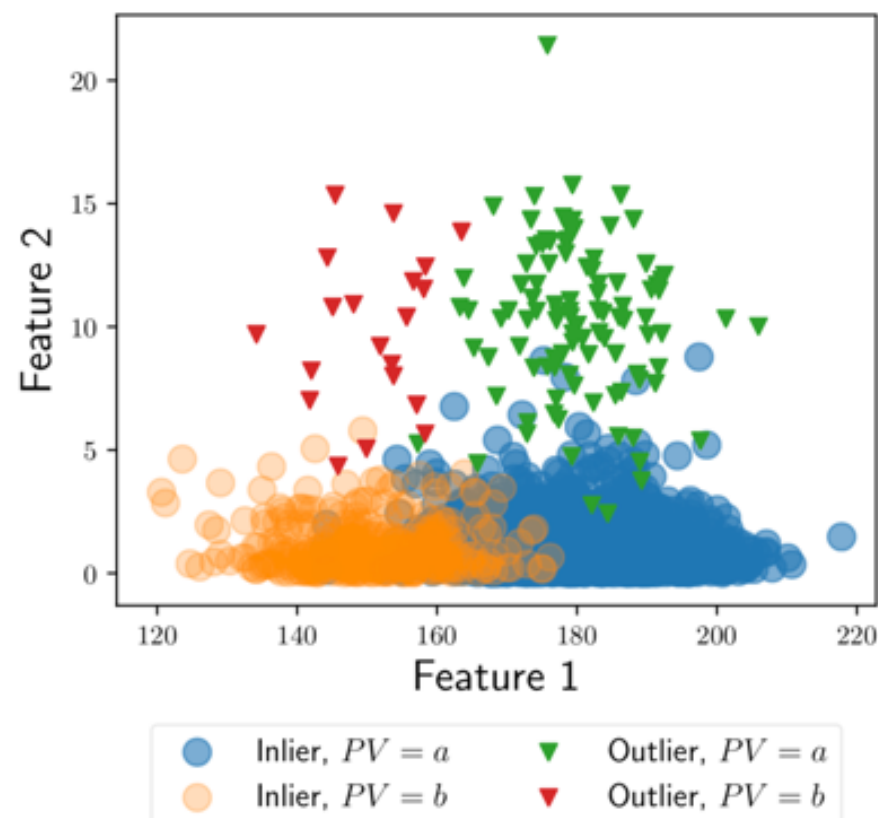
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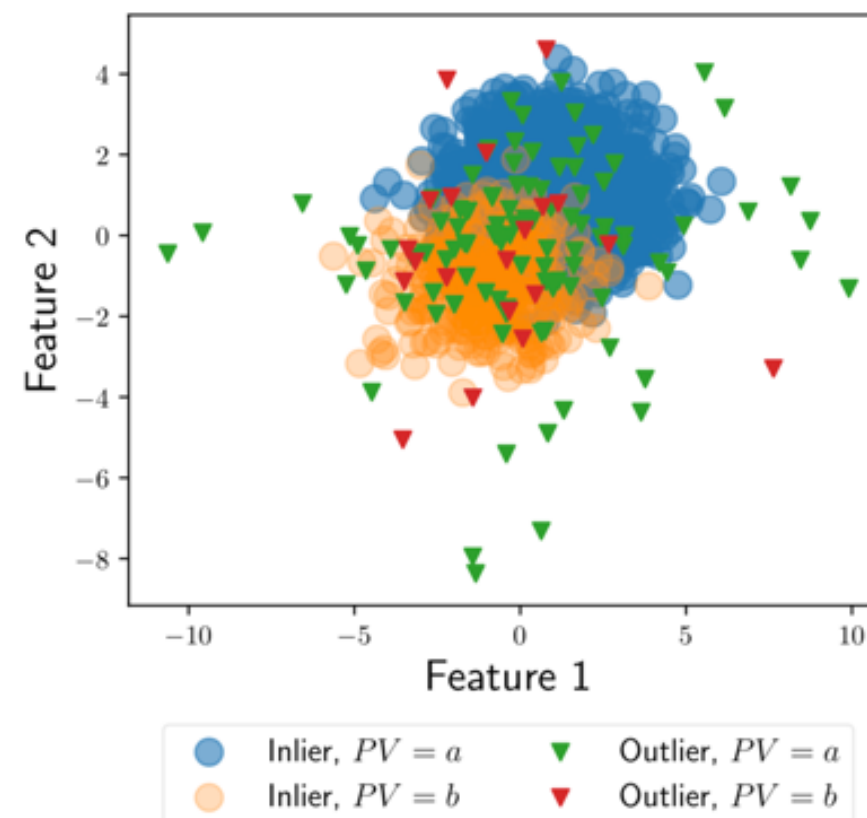
# Datasets

Dataset	N	d	PV	PV = b	$ \mathcal{X}_{PV=a} / \mathcal{X}_{PV=b} $	% outliers	Labels
Adult	25262	11	gender	<i>female</i>	4	5	{income $\leq$ 50K, income $>$ 50K}
Credit	24593	1549	age	<i>age <math>\leq</math> 25</i>	4	5	{paid, delinquent}
Tweets	3982	10000	racial dialect	<i>African-American</i>	4	5	{normal, abusive}
Ads	1682	1558	simulated	1	4	5	{non-ad, ad}
Synth1	2400	2	simulated	1	4	5	{0, 1}
Synth2	2400	2	simulated	1	4	5	{0, 1}

Synthetic  
datasets



Synth1



Synth2



# Baselines

- BASE – fairness-agnostic deep anomaly detector

## Preprocessing based methods

- RW – reweights instances [\[Kamiran et al.'2012\]](#)
- DIR – edits features to de-correlate PV [\[Feldman et al.'2015\]](#)
- LFR – latent representation obfuscating PV information [\[Zemel et al.'2013\]](#)
- ARL – latent representation via adversarial training [\[Beutel et al.'2017\]](#)

# Evaluation Measures

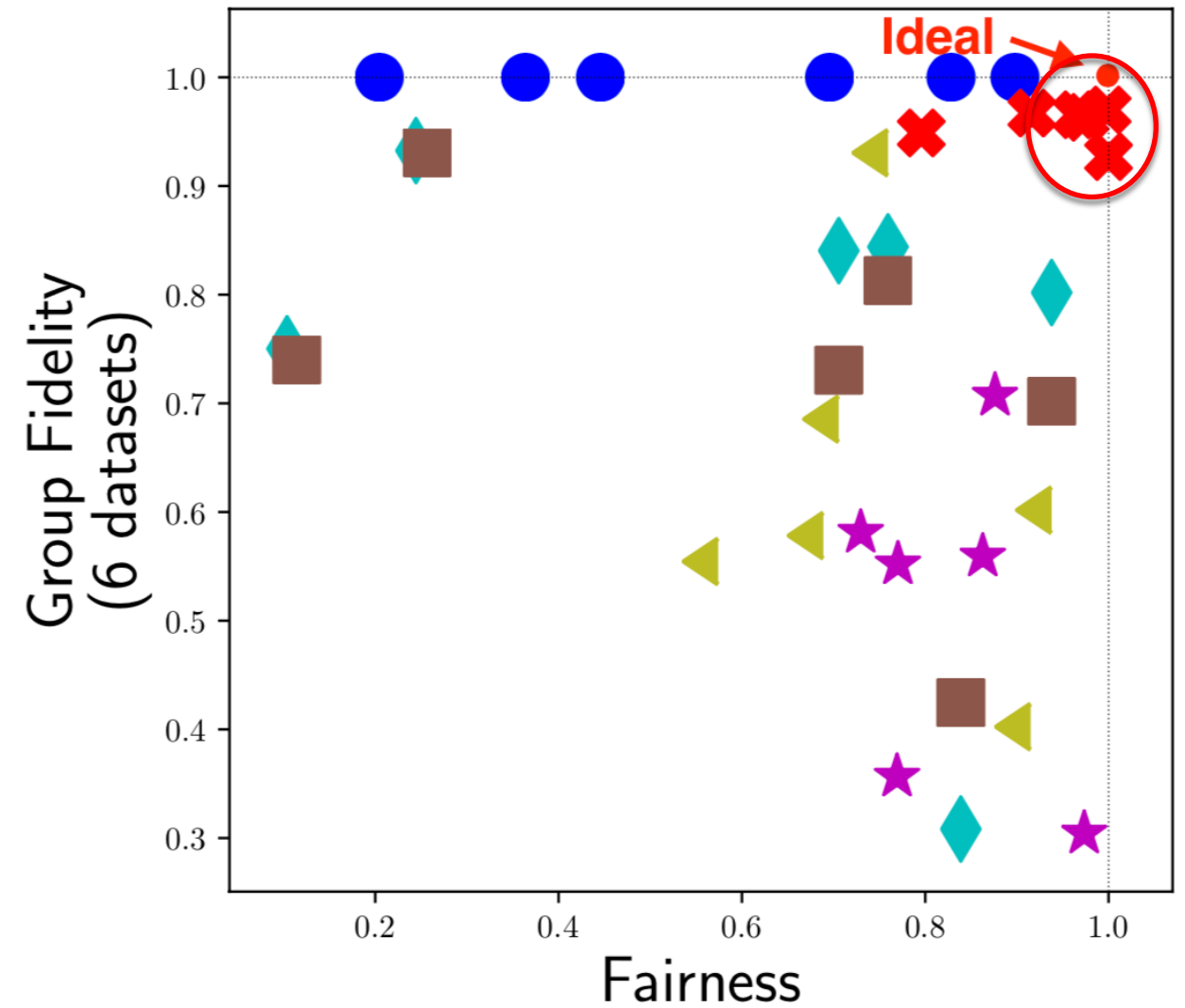
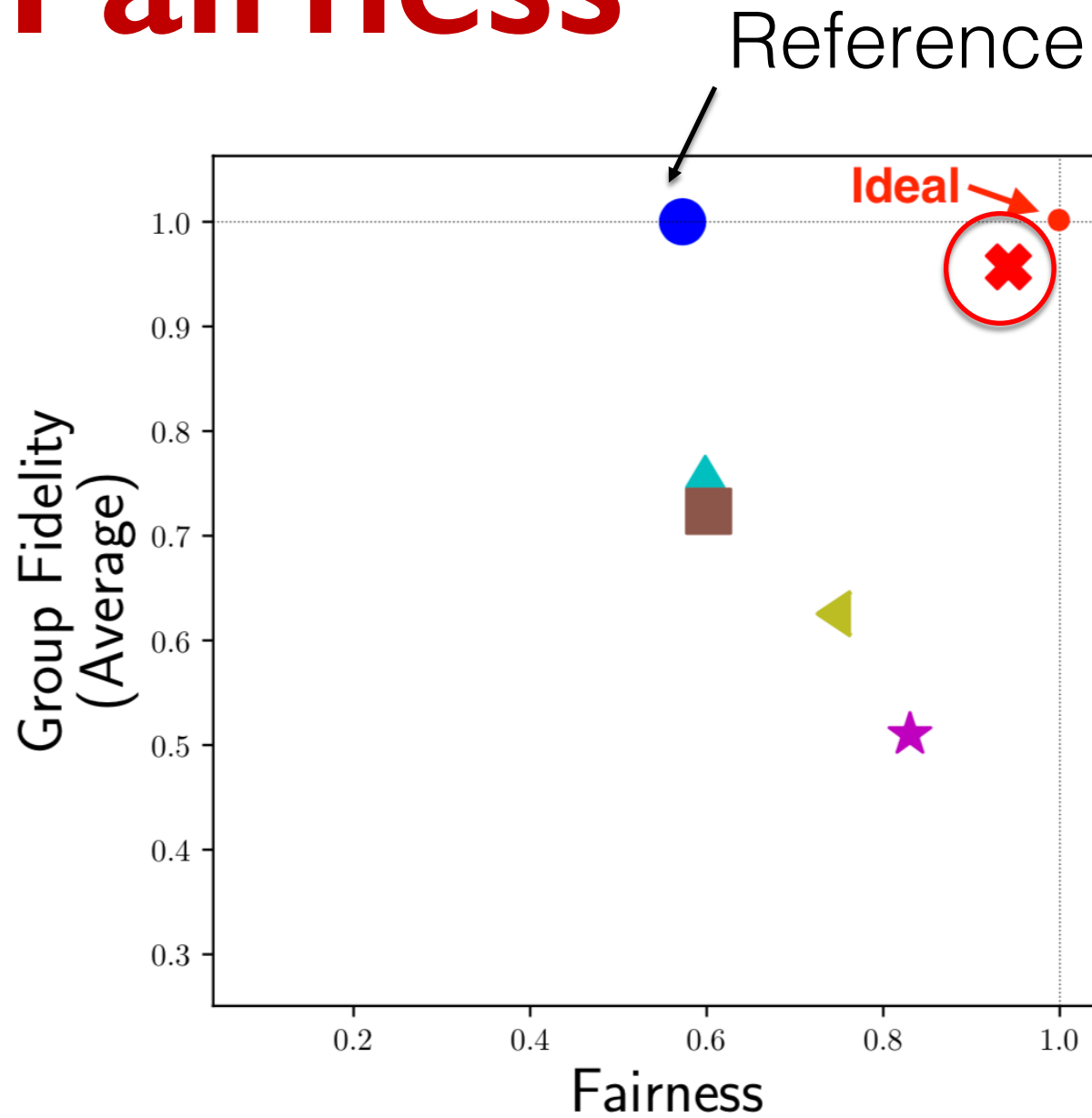
- Fairness =  $\min\left(r, \frac{1}{r}\right)$ , where  $r = \frac{P(O=1|PV=a)}{P(O=1|PV=b)}$  [D3]

- Group Fidelity =  $HM(NDCG_{PV=a}, NDCG_{PV=b})$  [D4]

- AUC-ratio =  $\frac{AUC_{PV=a}}{AUC_{PV=b}}$
- AP-ratio =  $\frac{AP_{PV=a}}{AP_{PV=b}}$

Label-aware parity measures  
used when ground-truth  
labels are available

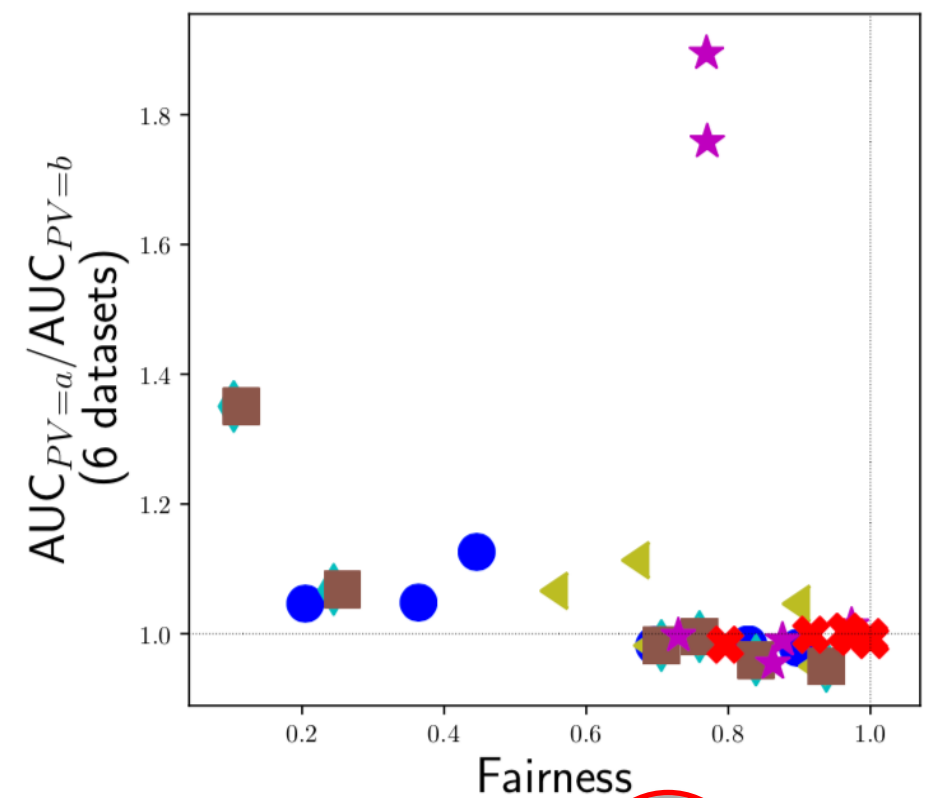
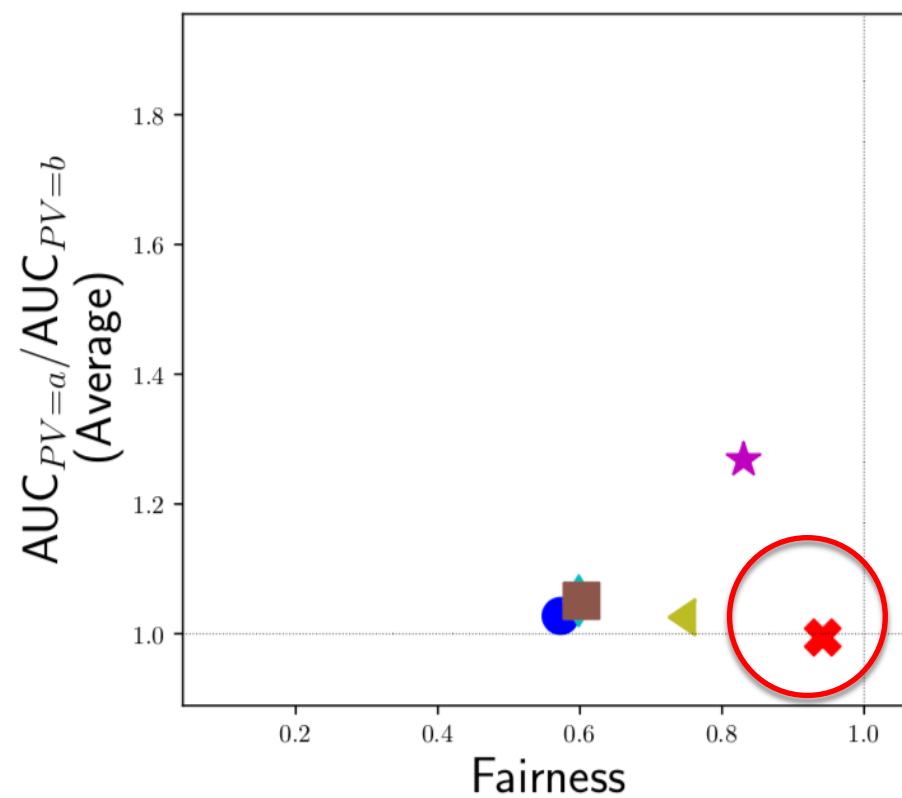
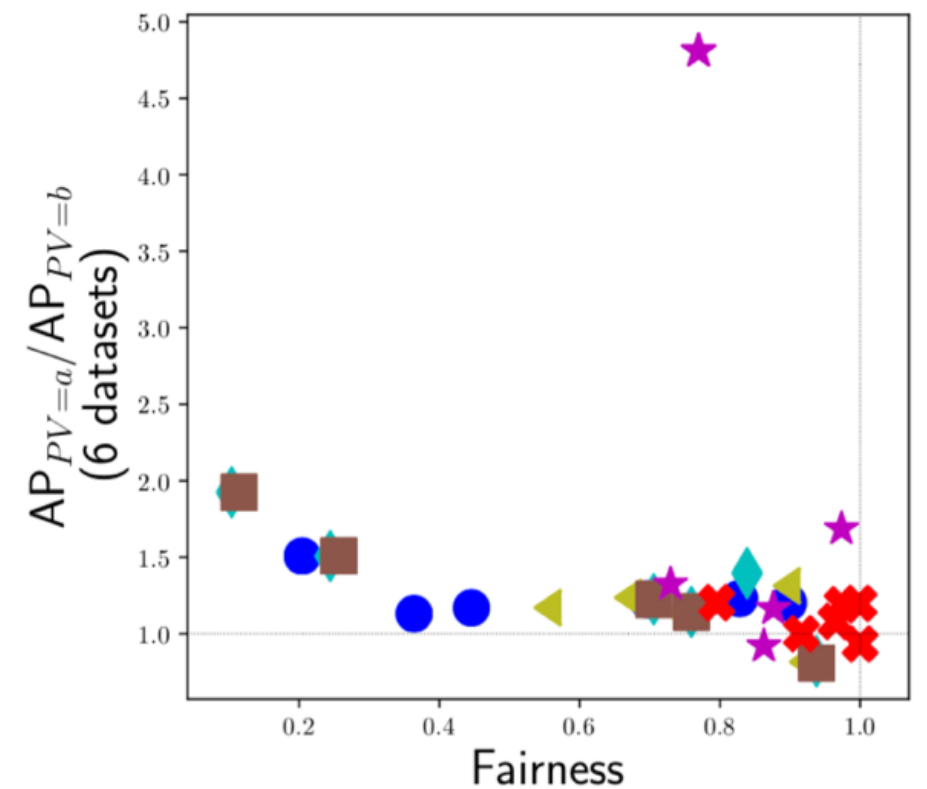
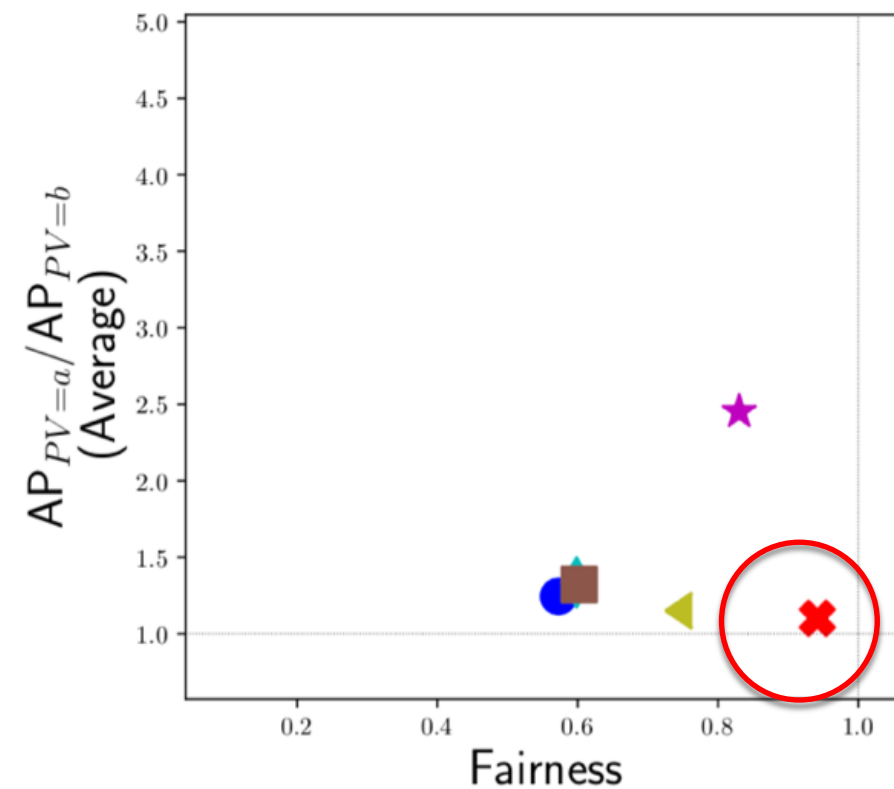
# Fairness



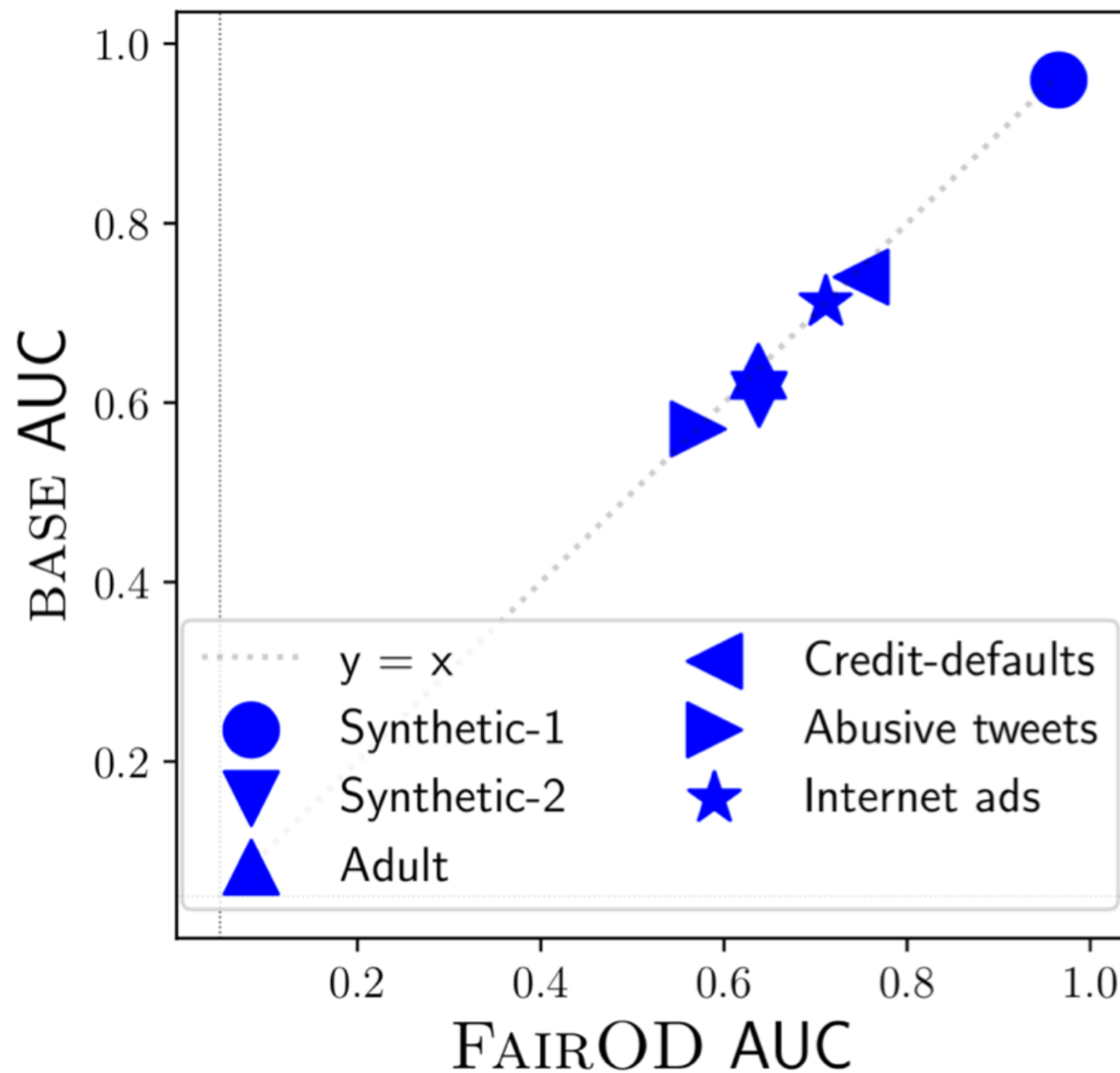
## Group Fidelity vs Fairness

# Fairness

## Label-aware parity measures vs Fairness

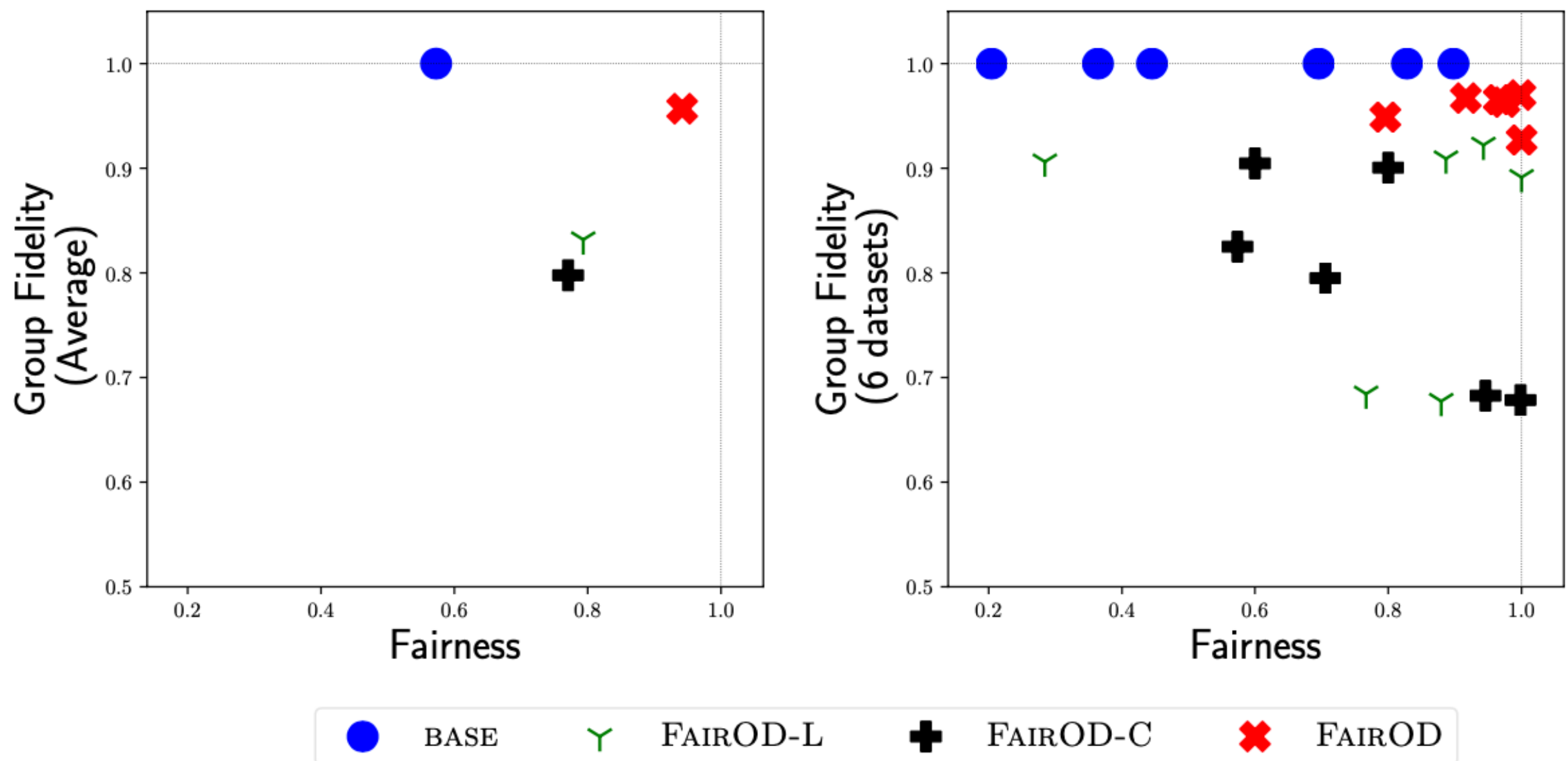


# Fairness-accuracy trade-off



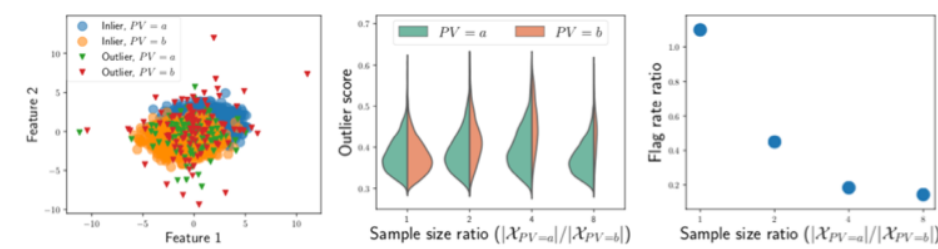
# Ablation study

- FairOD-**L** : only SP-based regularization (permits “**L**aziness”)
- FairOD-**C** : **C**orrelation-based group fidelity regularization



# Conclusion

- ✓ Guiding desiderata for, and concrete formalization of the fair OD problem



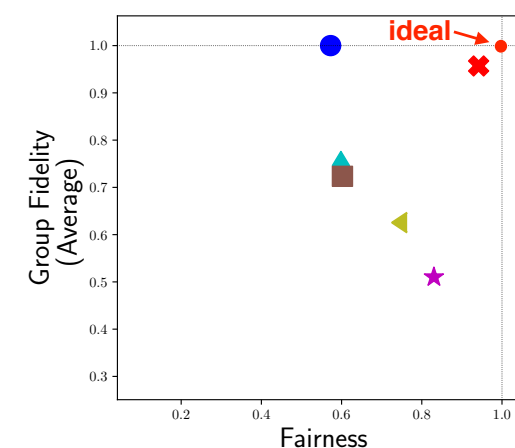
- ✓ Introduced well-motivated fairness criteria



- ✓ Proposed FAIROD

$$\mathcal{L} = \underbrace{\alpha \mathcal{L}_{\text{BASE}}}_{\text{Reconstruction}} + (1 - \alpha) \underbrace{\mathcal{L}_{\text{SP}}}_{\text{Statistical Parity}} + \gamma \underbrace{\mathcal{L}_{\text{GF}}}_{\text{Group Fidelity}}$$

- End-to-end detector w/ prescribed criteria
- Accurate detection that achieves fairness goals



# Code, paper, and slides



<https://tinyurl.com/fairOD>

## Thanks!



Carnegie Mellon University  
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